# Searching for Extra Dimensions at the Tevatron





(For the CDF & DØ Collaborations)

**SSI '04** 

August 9, 2004

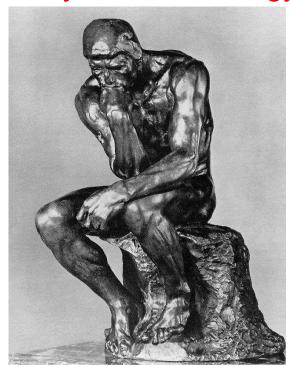






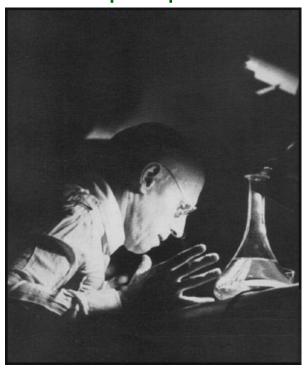
## **Out-Sketch**

### Theory/Phenomenology Tabletop Experiments



See Tom Rizzo's Talk:

- Models
- Cosmology Constraints
- Future



See Sylvia Smullin's Talk:

Gravity at short distances

### **Accelerator Searches**



#### This Talk:

- Brief Theory Recap
- Tevatron & Detectors
- Searches:
  - o ADD Model
  - o TeV<sup>-1</sup> Scenario
  - o RS Model
  - o Universal ED
  - o Use-Them-n-Lose-Them ED (little Higgs models)
- Conclusions



# Big Why? (Or Math Meets Physics)

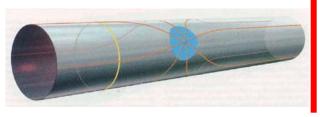
- Math physics: some dimensionalities are quite special
- Example: Laplace equation in two dimensions has logarithmic solution; for any higher number of dimensions it obeys power law instead
- Some of these peculiarities exhibit themselves in condensed matter physics, e.g. diffusion equation solutions allow for long-range correlations in 2D-systems (cf. flocking)
- Modern view in topology: one dimension is trivial; two and three spatial dimensions are special (properties are defined by the topology); any higher number is not
- Do we live in a special space, or only believe that we are special?



# Difference Between the Models

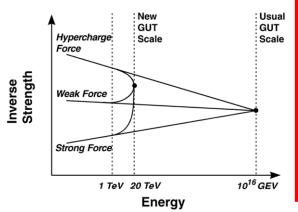
#### ADD Model:

- \*Eliminates" the hierarchy problem by stating that physics ends at a TeV scale
- Only gravity lives in the "bulk" space
- Size of ED's (n=2-7) between ~100 μm and ~1 fm
- Doesn't explain how to make ED large



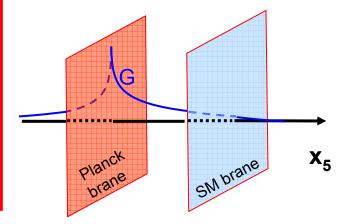
#### TeV-1 Scenario:

- Lowers GUT scale by changing the running of the couplings
- Only gauge bosons
   (g/γ/W/Z) propagate in
   a single ED; gravity is
   not in the picture
- Size of the ED ~1 TeV⁻¹ or ~10⁻¹⁰ m



### RS Model:

- A rigorous solution to the hierarchy problem via localization of gravity
- Gravitons (and possibly other particles)
   propagate in a single ED,
   w/ special metric
- Size of this ED as small as ~1/M<sub>Pl</sub> or ~10<sup>-35</sup> m

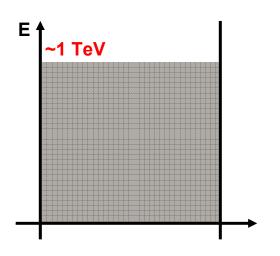




# Kaluza-Klein Spectrum

### **ADD Model:**

- Winding modes with energy spacing  $\sim 1/r$ , i.e. 1 meV - 100 MeV
- Can't resolve these modes – they appear as continuous spectrum



### TeV-1 Scenario:

- Winding modes with nearly equal energy spacing ~1/r, i.e. ~TeV
- Can excite individual modes at colliders or look for indirect effects

$$M_{i} = \sqrt{M_{0}^{2} + i^{2}/r^{2}}$$

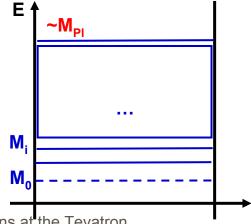
$$M_{i}$$

$$M_{0}$$

### **RS Model:**

- "Particle in a box" with a special metric
- Energy eigenvalues are given by zeroes of Bessel function J₁
- Light modes might be accessible at colliders

$$\begin{split} M_i &= M_0 \, x_i / x_0 \approx M_0, 1.83 M_0, \\ 2.66 M_0, 3.48 M_0, 4.30 M_0, \dots \\ & \text{E} \, \uparrow \quad & \text{I} \end{split}$$



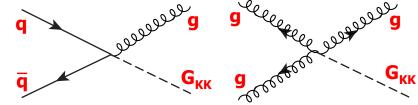


# Collider Signatures for Large Extra Dimensions

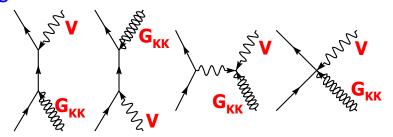
- Kaluza-Klein gravitons couple to the energy-momentum tensor, and therefore contribute to most of the SM processes
- **♣** For Feynman rules for  $G_{KK}$  see:
  - Han, Lykken, Zhang, PR **D59**, 105006 (1999)
  - Giudice, Rattazzi, Wells, Nucl. Phys. **B544**, 3 (1999)
- Since graviton can propagate in the bulk, energy and momentum are not conserved in the G<sub>KK</sub> emission from the point of view of our 3+1 space-time
- Depending on whether the G<sub>KK</sub> leaves our world or remains virtual, the collider signatures include single photons/Z/jets with missing E<sub>T</sub> or fermion/vector boson pair production
- Graviton emission: direct sensitivity to the fundamental Planck scale M<sub>D</sub>
- Virtual effects: sensitive to the ultraviolet cutoff M<sub>S</sub>, expected to be ~M<sub>D</sub> (and likely < M<sub>D</sub>)
- The two processes are complementary

### Real Graviton Emission

Monojets at hadron colliders

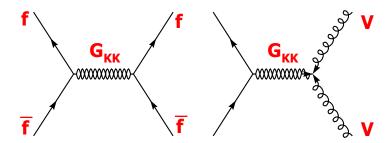


Single VB at hadron or e<sup>+</sup>e<sup>-</sup> colliders



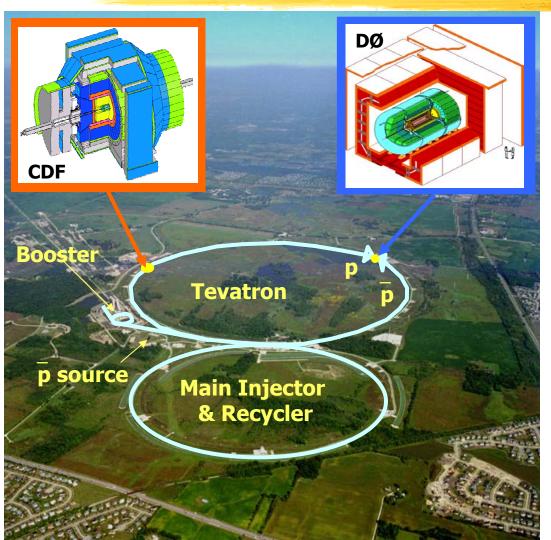
#### Virtual Graviton Emission

Fermion or VB pairs at hadron or e<sup>+</sup>e<sup>-</sup> colliders





### **Run II Vital Statistics**

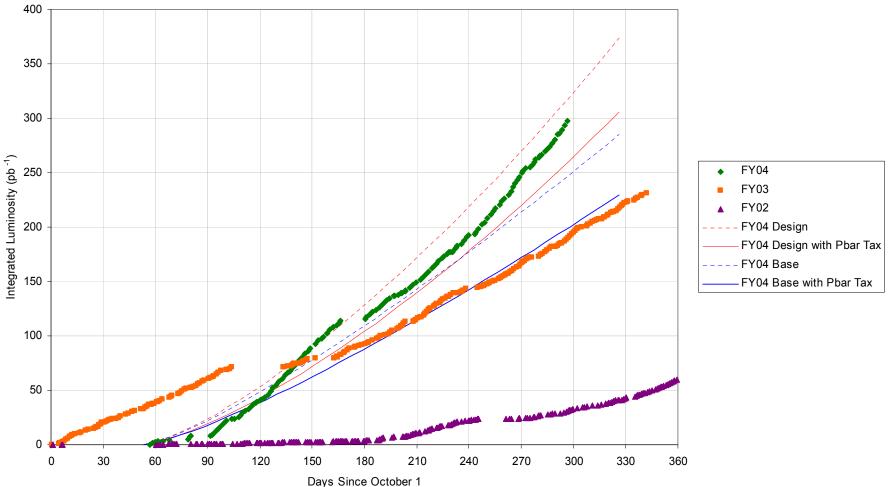


- Significant upgrade of the detectors and the accelerator complex:
  - New main injector and antiproton recycler
  - Higher c.o.m. energy: (1.8 TeV → 1.96 TeV)
  - Shorter bunch crossing:  $(3.5 \mu s \rightarrow 396 ns)$
  - More proton and antiproton bunches: (6 x 6 → 36 x 36)
  - Projected integrated luminosity per experiment:
    - ♣ ~2 fb<sup>-1</sup> (2006)
    - **♣** ~8 fb<sup>-1</sup> (2009)
- Slow start but we caught up!
- Highest luminosity so far: 1.03 x 10<sup>32</sup> cm<sup>-2</sup>s<sup>-1</sup>
- Nearly 0.5 fb<sup>-1</sup> of data on tape per experiment to date
- ♣ Data taking efficiency: 85-90%



## **Tevatron Performance**



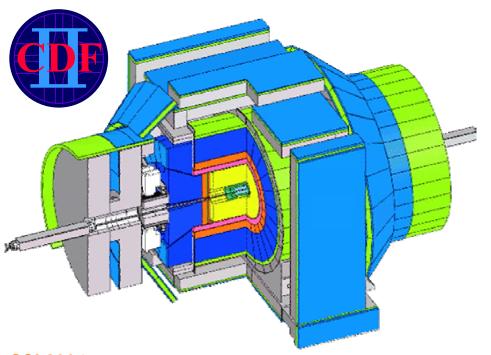


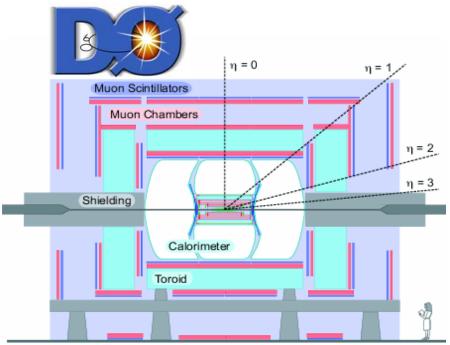


## CDF and DØ

- New:
  - ❖ silicon detector, drift chamber
  - ❖ TOF PID system
- Upgraded:
  - calorimeter, muon system
  - DAQ/trigger, displaced-vertex trigger

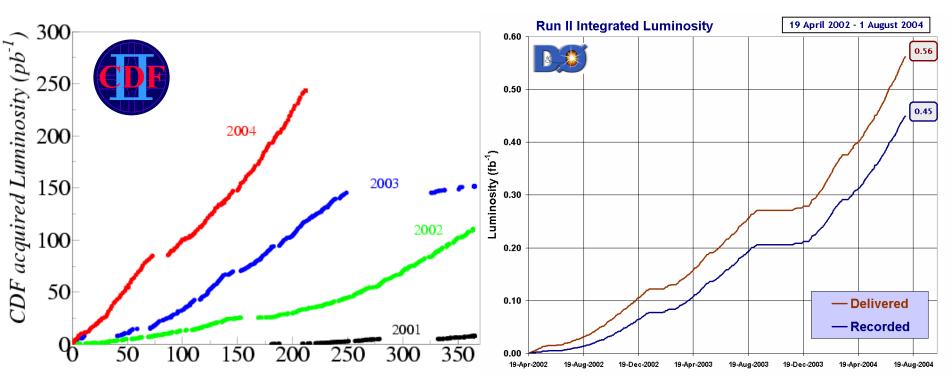
- New:
  - 2T superconducting solenoid
  - ❖ silicon detector, fiber tracker
- Upgraded:
  - ❖ FE electronics, muon system
  - DAQ/trigger, displaced-vertex trigger







# **CDF & DØ Performance**



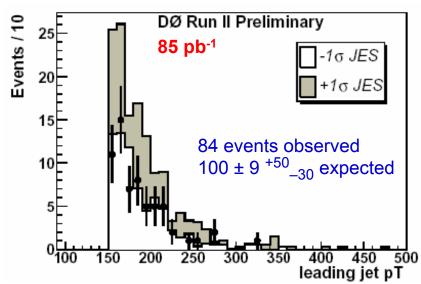
1 billion events recorded as of August 2!

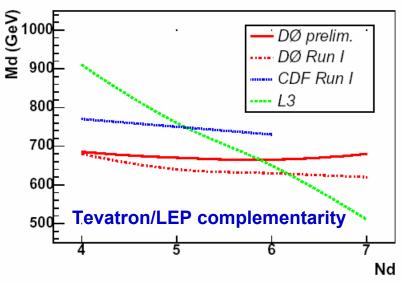
- ❖ Both experiments are ≈85% efficient over the last year
- ❖ Most of the analyses shown in this talk are based on ~200 pb⁻¹, which corresponds to 2002-2003 data



# **Search for Monojets**

- **♣** Challenge: large instrumental background from ME<sub>T</sub> mismeasurement and cosmics
- Irreducible physics background from Z(vv) + jet(s): forced to use high jet  $P_T$ ,  $ME_T$  cuts
- **♣** Pioneered in Run I by DØ [PRL **90**, 251802 (2003)]:  $M_D > 0.63 0.89$  TeV (n=6-2)
- **Recently superseded by CDF** [PRL **92**, 121802 (2004)]:  $M_D > 0.71 1.00$  TeV (n=6-2)
- $\blacksquare$  CDF also pioneered similar search in  $\gamma$ +ME<sub>T</sub>, albeit less sensitive [PRL **89**, 281801 (2002)]
- New Run II analysis from DØ based on 85 pb⁻¹ of data collected with special trigger
  - Major systematics from jet energy scale to be reduced soon
  - Sensitivity already exceeds that for DØ in Run I, but still below the CDF's Run I result
  - ♣ Impressive sensitivity already achieved with less data due to superior detector and higher energy

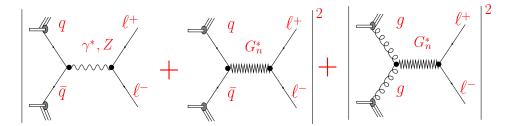






## Virtual Graviton Effects

♣ In the case of pair production via virtual graviton, gravity effects interfere with the SM (e.g., l+l⁻ at hadron colliders):



♣ Therefore, production cross section has three terms: SM, interference, and direct gravity effects:

$$\frac{d^2\sigma}{d\cos\theta^*dM} = \frac{d^2\sigma_{SM}}{d\cos\theta^*dM} + \frac{a(n)}{M_S^4} f_1(\cos\theta^*, M) + \frac{a(n)^2}{M_S^8} f_2(\cos\theta^*, M)$$

- ★ The sum in KK states is divergent in the effective theory, so in order to calculate the cross sections, an explicit cut-off is required
- ♣ An expected value of the cut-off  $M_S \approx M_D$ , as this is the scale at which the effective theory breaks down, and the string theory needs to be used to calculate production
- There are three major conventions on how to write the effective Lagrangian:
  - Hewett, Phys. Rev. Lett. 82, 4765 (1999)
  - Giudice, Rattazzi, Wells, Nucl. Phys. B544, 3 (1999); revised version, hepph/9811291
  - Han, Lykken, Zhang, Phys. Rev. **D59**, 105006 (1999); revised version, hep-ph/9811350
- ♣ Fortunately all three conventions turned out to be equivalent and only the definitions of M<sub>S</sub> are different



# Hewett, GRW, and HLZ Formalisms

- Hewett: neither sign of the interference nor the dependence on the number of extra dimensions is known; therefore the interference term is  $\sim \lambda/M_S^4$ (Hewett), where  $\lambda$  is of order 1; numerically uses  $\lambda = \pm 1$
- GRW: sign of the interference is fixed, but the dependence on the number of extra dimensions is unknown; therefore the interference term is  $\sim 1/\Lambda_T^4$  (where  $\Lambda_T$  is their notation for M<sub>S</sub>)
- **HLZ**: not only the sign of interference is fixed, but the n-dependence can be calculated in the effective theory; thus the interference term is ∼ 𝒯/M<sub>S</sub>⁴(HLZ), where 𝒯 reflects the dependence on the number of extra dimensions:

$$F = \begin{cases} \log\left(\frac{M_S^2}{s}\right), n = 2\\ \frac{2}{n-2}, n > 2 \end{cases}$$

Correspondence between the three formalisms:

$$M_S(\text{Hewett})|_{\lambda=+1} \equiv \sqrt[4]{\frac{2}{\pi}} \Lambda_T(\text{GRW})$$

$$\frac{\lambda}{M_S^4(\text{Hewett})} = \frac{\pi}{2} \frac{\mathcal{F}}{M_S^4(\text{HLZ})}$$

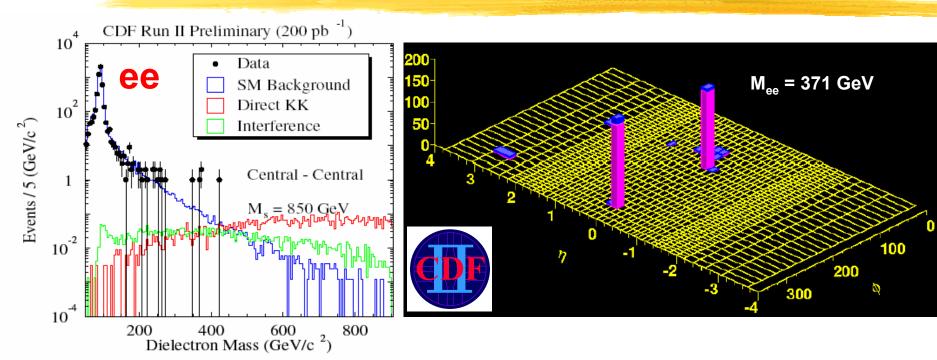
$$\frac{1}{\Lambda_T^4(\mathbf{GRW})} = \frac{\mathcal{F}}{M_S^4(\mathbf{HLZ})}$$

**Rule** of thumb:

$$M_S(\text{Hewett})\Big|_{\lambda=+1} \approx M_S(\text{HLZ})\Big|_{n=5}$$
  
 $\Lambda_T(\text{GRW}) = M_S(\text{HLZ})\Big|_{n=4}$ 



# CDF Search for Virtual Graviton Effects



| CDF Run II Preliminary (200 pb <sup>-1</sup> ) |                             |               |               |               |       |       |       |       |       |       |   |
|------------------------------------------------|-----------------------------|---------------|---------------|---------------|-------|-------|-------|-------|-------|-------|---|
|                                                | $\eta_{95}$                 |               | Hewett        |               | HLZ   |       |       |       |       | GRW   |   |
|                                                | $(10^{-12} {\rm GeV}^{-4})$ |               | (GeV)         |               | (GeV) |       |       |       |       | (GeV) |   |
|                                                | $\lambda < 0$               | $\lambda > 0$ | $\lambda < 0$ | $\lambda > 0$ | n = 3 | n = 4 | n = 5 | n = 6 | n = 7 |       |   |
| Central-Central                                | 1.05                        | 1.18          | 987           | 959           | 1315  | 1105  | 999   | 929   | 879   | 1105  | ) |
| Central-Plug                                   | 2.23                        | 2.47          | 818           | 797           | 1089  | 916   | 827   | 770   | 728   | 916   |   |
| Combined                                       | 1.05                        | 1.18          | 987           | 959           | 1315  | 1105  | 999   | 929   | 879   | 1105  | ) |

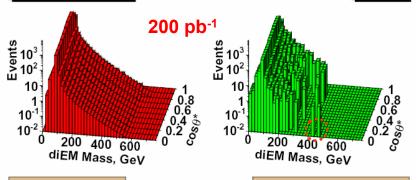


# DØ Search for Virtual Graviton Effects

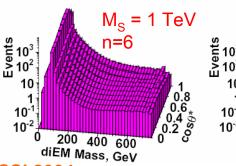
- Combine diphotons and dielectrons into "di-EM objects" to maximize efficiency
- High-mass, low |cosθ\*| tail is a characteristic signature of LED [Cheung, GL, PRD 62 076003 (2000)]

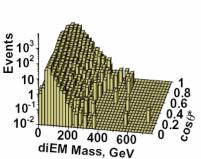
**SM Prediction | DØ Run II Preliminary** 











- Sensitivity is dominated by the diphoton channel  $(2 \rightarrow 1 + 1)$
- ♣ Data agree well with the SM predictions; proceed with setting limits on large ED: alone or in combination with our Run I result [PRL 86, 1156 (2001)]:

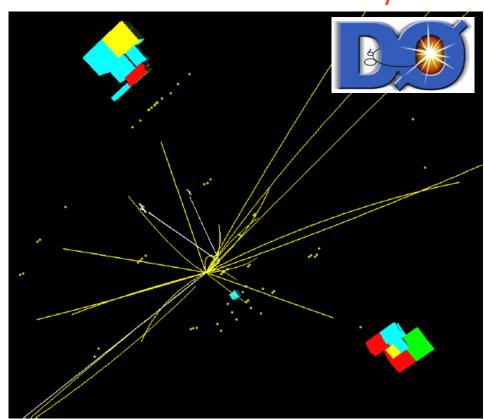
| Hewett |               | GRW              | HLZ              |           |           | (TeV, @95% CL) |          |           |  |
|--------|---------------|------------------|------------------|-----------|-----------|----------------|----------|-----------|--|
| λ = +1 | <i>λ</i> = −1 | Ortiv            | n = 2            | n = 3     | n = 4     | n = 5          | n = 6    | n = 7     |  |
| 1.22   | 1.10          | 1.36             | 1.56             | 1.61      | 1.36      | 1.23           | 1.14     | 1.08      |  |
| 1.28   | 1.16          | 1.43             | 1.67             | 1.70      | 1.43      | 1.29           | 1.20     | 1.14      |  |
|        |               | r <sub>max</sub> | <b>170</b><br>μm | 1.5<br>nm | 5.7<br>pm | 0.2<br>pm      | 21<br>fm | 4.2<br>fm |  |

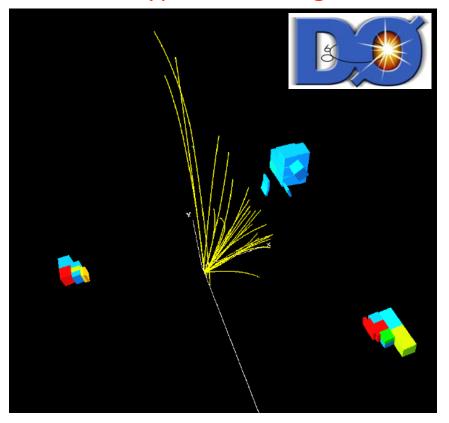
- ♣ These are the most stringent constraints on large ED for n > 2 to date, among all the experiments
- For n=2, the sensitivity is very close to that of the tabletop gravity measurements (M<sub>D</sub> = 1.7 TeV, r < 160 μm)</li>



## Interesting Candidate Events

■ While the DØ data are consistent with the SM, the two highest-mass candidates have anomalously low value of cosθ\* typical of ED signal:





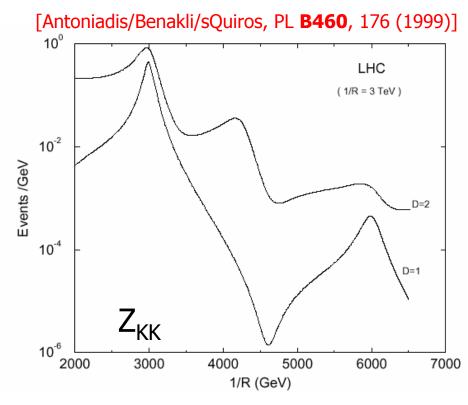
Event Callas:  $M_{ee} = 475 \text{ GeV}$ ,  $\cos \eta^* = 0.01$ 

 $M_{yy} = 436 \text{ GeV}, \cos \eta^* = 0.03$ 



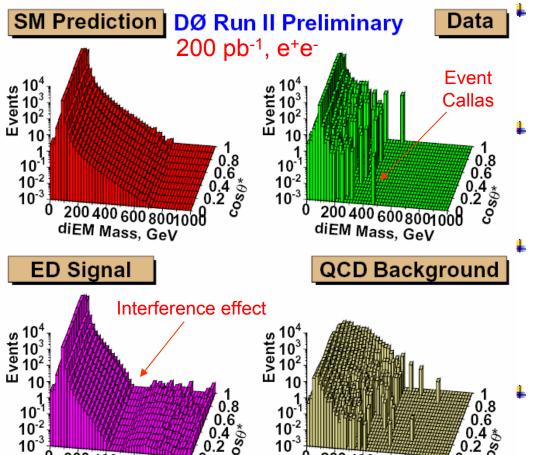
## **TeV<sup>-1</sup> Extra Dimensions**

- Intermediate-size extra dimensions with ~TeV-1 radius
- Introduced by Antoniadis [PL B246, 377 (1990)] in the string theory context; used by Dienes/Dudas/Gherghetta [PL B436, 55 (1998)] to allow for low-energy unification
  - ♣ Expect Z<sub>KK</sub>, W<sub>KK</sub>, g<sub>KK</sub> resonances at the LHC energies
  - At lower energies, can study effects of virtual exchange of the Kaluza-Klein modes of vector bosons
- Current indirect constraints come from precision EW measurements:
   1/r ~ 6 TeV
- No dedicated experimental searches at colliders to date





# First Dedicated Search for TeV<sup>-1</sup> Extra Dimensions



diEM Mass, GeV

- While the Tevatron sensitivity is inferior to the indirect limit, it's searching for effects of virtual KK modes, as they are complementary to those in the EW data
- DØ has performed the first dedicated search of this kind in the dielectron channel based on 200 pb<sup>-1</sup> of Run II data  $(Z_{KK}, \gamma_{KK} \rightarrow e^+e^-)$
- The 2D-technique similar to the search for ADD effects in the virtual exchange yields the best sensitivity in the DY production [Cheung/GL, PRD **65**, 076003 (2002)]
- Data agree with the SM predictions, which resulted in the following limit on their size:
  - ♣ 1/r > 1.12 TeV @ 95% CL
  - $r < 1.75 \times 10^{-19} \text{ m}$

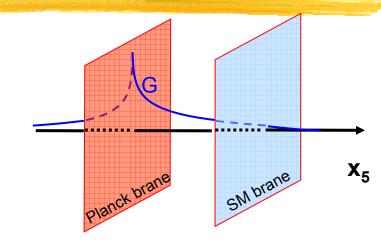
diEM Mass, GeV

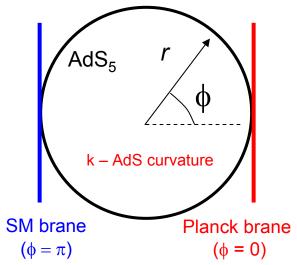
1/r = 0.8 TeV



# Randall-Sundrum Scenario

- Randall-Sundrum (RS) scenario [PRL **83**, 3370 (1999); PRL **83**, 4690 (1999)]
  - ♣ + brane no low energy effects
  - +- branes TeV Kaluza-Klein modes of graviton
  - Low energy effects are given by  $\Lambda_{\pi}$ ; for  $kr_c \sim 10$ ,  $\Lambda_{\pi} \sim 1$  TeV and the hierarchy problem is solved naturally
  - **4** Zero-mode coupling is suppressed as  $1/M_{Pl}$ ; other modes are coupled as  $1/Λ_T$





$$ds^{2} = e^{-2kr|\phi|} \eta_{\mu\nu} dx^{\mu} dx^{\nu} - r^{2} d\phi^{2}$$
$$\Lambda_{\pi} = \overline{M}_{Pl} e^{-kr\pi}$$

Reduced Planck mass:

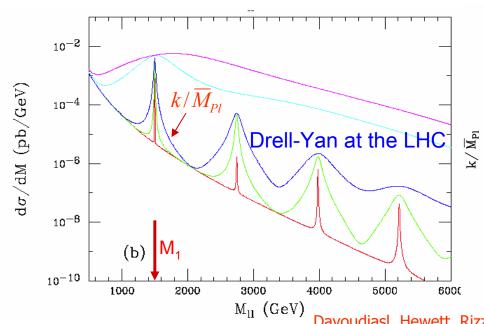
$$\overline{M}_{Pl} \equiv M_{Pl} / \sqrt{8\pi}$$

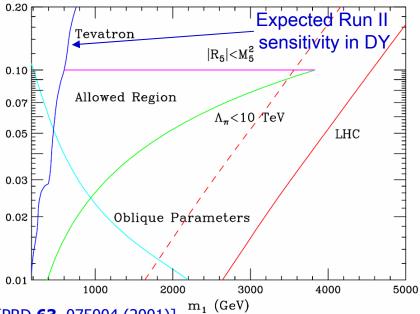


## **Model Parameters**

- Need only two parameters to define the model: k and r<sub>c</sub>
- Equivalent set of parameters are:
  - ♣ The mass of the first KK mode, M₁
  - Dimensionless coupling  $k/M_{pl}$

- To avoid fine-tuning and nonperturbative regime, coupling can't be too large or too small
- $0.01 \le k / \overline{M}_{Pl} \le 0.10$  is the expected range
- Gravitons are narrow



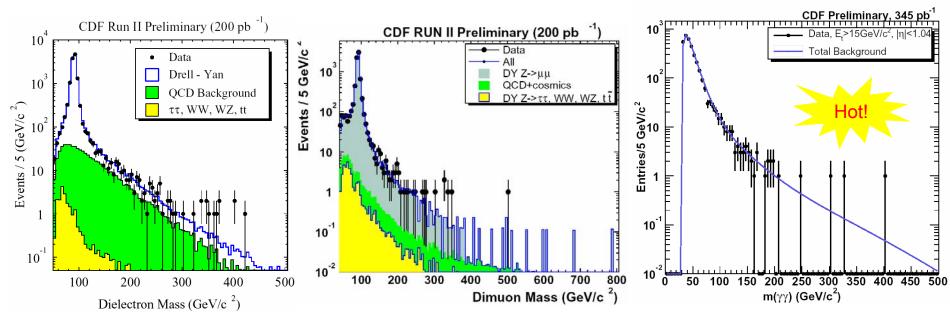


Davoudiasl, Hewett, Rizzo [PRD 63, 075004 (2001)]



## **CDF Search for RS Gravitons**

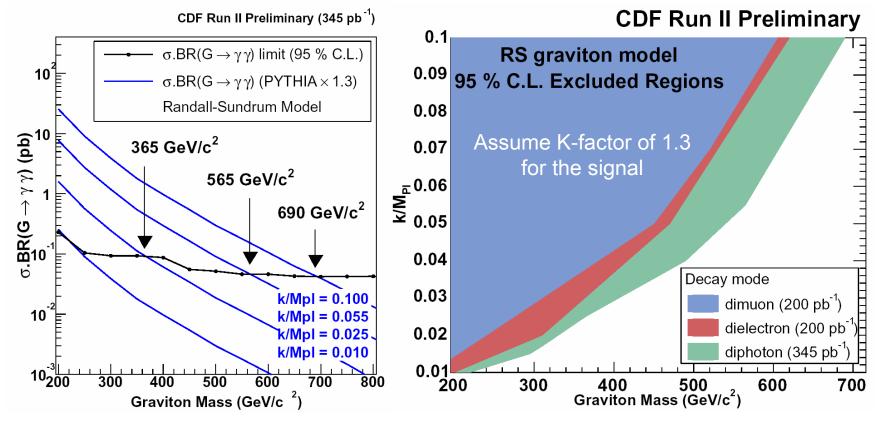
- CDF pioneered these search in 2003
- **4** Based on e<sup>+</sup>e<sup>-</sup>,  $\mu$ <sup>+</sup> $\mu$ <sup>-</sup> (200 pb<sup>-1</sup>) and  $\gamma\gamma$  (345 pb<sup>-1</sup>, central photons only) modes
- **♣** N.B.: B(G  $\rightarrow$  gg)  $\approx$  2B(G  $\rightarrow$  e<sup>+</sup>e<sup>-</sup>); diphotons also have higher acceptance
- Counting experiment in a resolution-driven sliding window in mass
- Data agree with expected SM background
- Interpret this as a search for narrow RS gravitons to set limits on the model parameters





# **CDF Limits on RS Model**

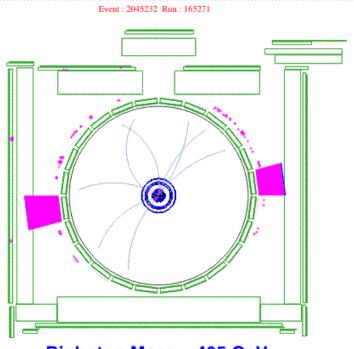
- Sensitivity is driven by the diphoton channel
- Gravitons with masses up to 690 GeV have been excluded for the coupling of 0.10
- Further improvement can be achieved by combining three channels (to be done!)



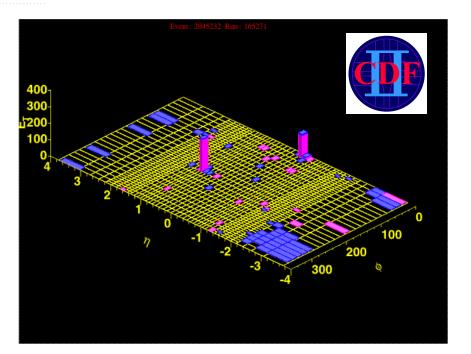


## The Highest Mass Diphoton Event

$$M_{\gamma\gamma} = 405 \text{ GeV}$$



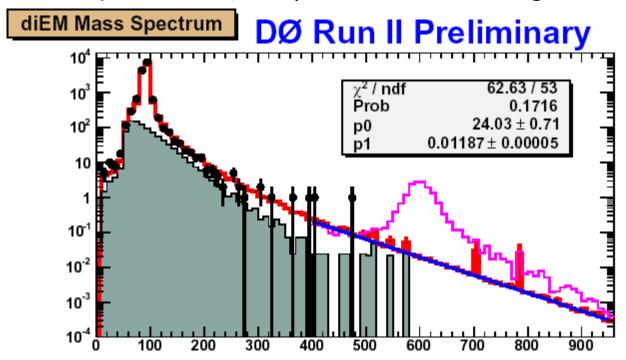
Diphoton Mass = 405 GeV Photon Et = 172, 175 GeV





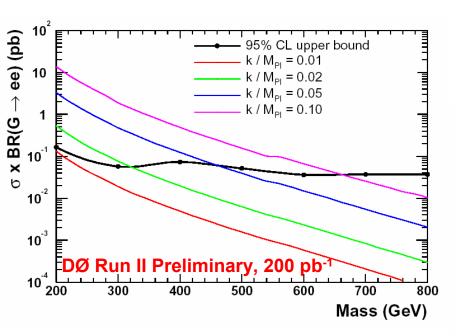
### **DØ Search for RS Gravitons**

- ♣ DØ has just completed similar analysis and produced first results
- ♣ Analysis based on 200 pb<sup>-1</sup> of e<sup>+</sup>e<sup>-</sup> data the same data set as used for searches for TeV<sup>-1</sup> ED
- Search window size has been optimized to yield maximum signal significance
- Analysis technique is similar; acceptance is somewhat higher



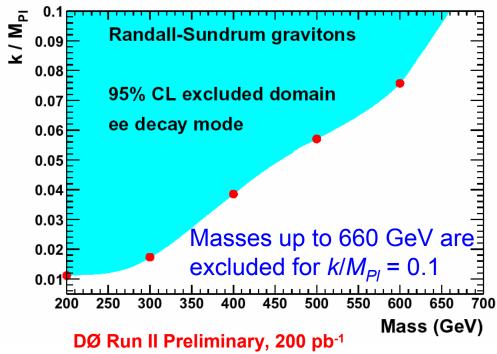


# DØ Limits in the Dielectron Channel



Cross section scales as  $(k/M_{Pl})^2$ 







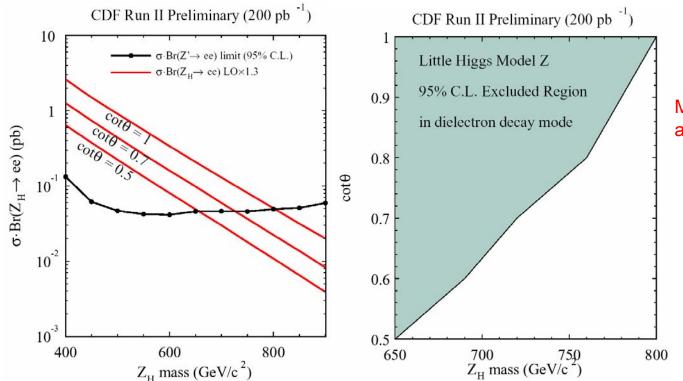
### **Almost No Extra Dimensions**

- Novel idea: build a multidimensional theory that is reduced to a fourdimensional theory at low energies [Arkani-Hamed, Cohen, Georgi, Phys. Lett. **B513**, 232 (1991)]
- An alternative EWSB mechanism, the so-called Little Higgs (a pseudo-goldstone boson, responsible for the EWSB) [Arkani-Hamed, Cohen, Katz, Nelson, JHEP 0207, 034 (2002)]
- Limited low-energy phenomenology: one or more additional vector bosons; a charge +2/3 vector-like quark (decaying into V/h+t), necessary to cancel quadratic divergencies), possible additional scalars (sometimes even stable!), all in a TeV range
- Unfortunately, the Tevatron reach is not very large; LHC would be the machine to probe this model
- However: started looking for this types models as a part of more generic search for Z'



# CDF Limit On Z<sub>H</sub>

- Littlest Higgs model: an additional gauge boson Z<sub>H</sub> with the SU(2) coupling parameter cotθ
   [Han, Logan, McElrath, Wang, PRD 67, 095004 (2003)]
- $\blacksquare$  Search done in the  $e^+e^-$ ,  $\mu^+\mu^-$  (200 pb<sup>-1</sup>) mode; best sensitivity is in dielectrons
- Straight extension of the RS graviton/Z' analyses
- Limits are far from theoretically motivated masses, but a good start!



Masses up to 800 GeV are excluded for  $\cot \theta = 1$ 



## **Conclusions**

- Colliders offer ultimate probe of models with extra spatial dimensions
- Tevatron is the highest-energy machine today and has an excellent opportunity to find first signs of extra dimensions in space
- Accelerator performance is excellent and both CDF and DØ have a large number of new results in this area
- Sensitivities beyond existing limits have been achieved already:
  - ♣ Tightest limits on large ED to date
  - ♣ First limits on RS gravitons
  - ♣ First test of Little Higgs models
- Stay tuned for more exciting results to come with much larger data set – any day now could bring an exciting discovery!

